



## **A STUDY ON USAGE OF SHARPE'S SINGLE INDEX MODEL IN PORTFOLIO CONSTRUCTION W.R.T NSE IT INDEX**

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### **Abstract**

*Portfolio management is a vital aspect of decision making process for any investor. It is crucial for the investor to take a call as to where to invest and how much to invest. The present study focuses on constructing the optimal portfolio with the help of Sharpe Single Index model. Sharpe Single index model uses various inputs such as excess return to beta ratio, unsystematic risk, market return and variance etc to construct the optimal portfolio. In present study, portfolio is constructed from IT stocks of NSE IT Index. Monthly data is collected from Ten IT companies of NSE IT for the time period of One Year from December 2016 to November 2017. Out of 10 stocks, 5 stocks are selected for investing namely MindTree (32.127%), Infibeam (4.30%), KPIT (17.761%), OFSS (26.117%) and Wipro (19.691%)*

**Keywords:** - Portfolio, Sharpe, Single Index Model

### **Introduction**

William Sharpe conceived and developed the Sharpe's Single Index model for portfolio formulation. Input variables for this model are significantly less than the model proposed by Harry Markowitz. Sharpe' Single Index model primarily presumes that a single factor known as index can explain the co – variance of the security. A particular version uses the market index such as S&P 500 as an independent variable. This model is called the market model. According to the market model, the performance of an asset or a security is related to the performance of the portfolio, which in turn varies as per the beta of the security.

All the securities are initially ranked according to the ratio of their excess return vs

beta according to this model. Further step is computation of a cut – off rate which is then compared with the ratio of excess return to beta to take an investment decision. Finally the proportion of investment to be made in each security comprising the portfolio is determined.

### **Literature review:**

A study named “Optimal Portfolio Construction in Stock Market – An Empirical Study on Selected Stocks in Manufacturing Sectors of India” was undertaken by (Dr. Sathya Swaroop Debasish, 2012). According to this research, any investment decision is highly influenced by risk and return. The researcher employed the Sharpe Single Index model to create a portfolio. The data was gathered from NSE NIFTY and a portfolio was constructed from top 14 stocks. Upon analysis, three stocks “Hero MotoCorp”, “Tata Motors” and “Asian Paints” were chosen for portfolio optimization.

Another research undertaken by (Kapil Sen and CA Disha Fattawat, 2014) also focused on Sharpe’s Single Index Model and its application in construction and creation of the portfolio. This study inferred that it is far simpler to construct a portfolio using Sharpe’s Single Index Model as compared to Mean – Variance Portfolio method formulated by Harry Markowitz.

A research by (Sarker, 2013) titled “Optimal Portfolio Construction: Evidence from Dhaka Stock Exchange in Bangladesh” also applied Sharpe’s Single Index model. He employed the model by utilizing monthly closing prices of about 164 companies which were listed on Dhaka Stock Exchange (DSE) between July 2007 and June 2012. He found that seven organizations were giving negative returns and 157 other companies showed positive returns.

### **Research methodology:**

The present study focuses on constructing the portfolio using Sharpe Single Index model. For this purpose, Ten IT companies of NSE IT Index as listed below are selected based on their weight. Monthly return for the last one year from 31<sup>st</sup> December 2016 to 30<sup>th</sup> November December 2017 and risk free rate of return is used for the calculation.

MINDTREE

INFIBEAM

KPIT

OFSS

Wipro

TechM

TCS

INFOSYS

HCLTECH

TATAELXSI

**Problem statement:**

An investor has to make very crucial and important decisions to maximize his returns. He needs to choose the assets/stocks/securities very judiciously and also decide on the quantum of investment to be made in each security. Therefore in this research, the problem faced by investors is which assets/stocks/securities to invest in and the proportion of investment in each security.

**Objective:**

To make the portfolio of NSE IT Index by using Sharpe Single Index model.

**Tools and techniques used for study:**

We employ Sharpe's Single Index model for portfolio construction and optimization.

**Sharpe Single Index Model Portfolio Construction**

**Step 1**

Ranking the securities based on excess return to beta ratio which is calculated as  $R_i - R_f / B_i$  where  $R_i$  means return of the security,  $R_f$  stands for risk free rate of return while  $B_i$  should be interpreted as systematic risk prevailing in the market.  $R_f = 8\%$

**Table 1: Ranking of securities based on excess Return to beta ratio**

Company Name	Mean Return $R_i$	Beta B	Unsystematic Risk $\sigma^2$	Excess Return $R_i - R_f$	$(R_i - R_f)/B$	Ranking
MINDTREE	0.26428153	0.20	0.05	0.18428153	0.903704613	1
INFIBEAM	0.257951667	0.22	0.39	0.177951667	0.826086272	2
KPIT	0.274407445	0.36	0.10	0.194407445	0.533305481	3
OFSS	0.232398233	0.73	0.04	0.152398233	0.209403869	4
Wipro	0.252869266	0.926578541	0.03565773	0.172869266	0.18656731	5
TechM	0.114829599	0.49	0.06	0.034829599	0.070727769	6
TCS	0.165821924	1.28	0.05	0.085821924	0.067292274	7
INFOSYS	0.108539788	1.39	0.05	0.028539788	0.020528709	8
HCLTECH	-1.58478734	2.05	2.91	-1.664787337	0.811715557	9
TATAELXSI	0.295109609	-0.22	0.08	0.215109609	0.995289571	10

**Step 2:**

**Calculating the cut off rate using following formula.**

Highest cut off rate will be regarded as  $C^*$ .

$$C_i = (\sigma_m^2 \cdot \sum ((R_i - R_f) \cdot B_i) / \sigma_{ei}^2) / (1 + \sigma_m^2 \cdot (\sum B_i^2 / \sigma_{ei}^2))$$

Where,  $\sigma_m^2$  = market variance,  $R_i - R_f$  = Market risk Premium,  $\sigma_{ei}^2$  = unsystematic risk

Market variance  $\sigma^2$  has been calculated on the basis of fluctuations in NSE IT Index from 31<sup>st</sup> December 2016 to 30<sup>th</sup> November 2017.  $\sigma^2=0.0232$

**Table 2: Calculation of systematic risk and cut – off rate Ci**

Name of the Company	$B^2/\sigma^2$	$B/\sigma^2$	$((R_i - R_F)/B) * B^2/\sigma^2$	$X = \text{Sum } B^2/\sigma^2$	$Y = \text{Sum } ((R_i - R_F)/B) * B^2/\sigma^2$	Cut Off
<b>MINDTREE</b>	0.762676	3.74011	0.68923 3995	0.76267 6	0.68923 3995	0.015778745
<b>INFIBEAM</b>	0.11858	0.55047	0.09795 7182	0.88125 6	0.78719 1177	0.017972505
<b>KPIT</b>	1.338395	3.67153	0.71377 3296	2.21965 1	1.50096 4474	0.033252686
<b>OFSS</b>	14.81487	20.3565	3.10229 0321	17.0345 2	4.60325 4794	0.076781048
<b>Wipro</b>	24.07747	25.9853	4.49206 8083	41.1119 8	9.09532 2878	0.108238385
<b>TechM</b>	4.130602	8.38793	0.29214 8238	45.2425 8	9.38747 1115	0.106480905
<b>TCS</b>	35.01892	27.4581	2.35650 2693	80.2615	11.7439 7381	0.095339944
<b>INFOYSYS</b>	35.50831	25.5412	0.72893 9864	115.769 8	12.4729 1367	0.078600079
<b>HCLTECH</b>	1.445056	0.70458	- 1.17297 4161	117.214 9	11.2999 3951	0.070565803
<b>TATAELXSI</b>	0.612493	-2.8339	- 0.60960 823	117.827 4	10.6903 3128	0.066504552

**Table 3: Selection of Securities. Securities whose  $((R_i - R_f)/B) > C_i$** 

Name of the Company	$(R_i - R_f)/B$	Cut Off	Decision
<b>MINDTREE</b>	0.903704613	0.015778745	<b>Selected</b>
<b>INFIBEAM</b>	0.826086272	0.017972505	<b>Selected</b>
<b>KPIT</b>	0.533305481	0.033252686	<b>Selected</b>
<b>OFSS</b>	0.209403869	0.076781048	<b>Selected</b>
<b>Wipro</b>	0.18656731	0.108238385	<b>Selected</b>
<b>TechM</b>	0.070727769	0.106480905	Rejected
<b>TCS</b>	0.067292274	0.095339944	Rejected
<b>INFOYSYS</b>	0.020528709	0.078600079	Rejected
<b>HCLTECH</b>	0.811715557	0.070565803	Rejected
<b>TATAELXSI</b>	0.995289571	0.066504552	Rejected

**Table 4: Proportion of Securities to be invested**

	A	B	A*B		
Name of the Company	$((R_i - R_f)/B) - C^*$	B/o2	Z <sub>i</sub>	$Z_i/\sum Z$	%
MINDTREE	0.887925868	3.740114363	3.320944294	0.321271295	32.127%
INFIBEAM	0.808113767	0.55047072	0.444842967	0.04303453	4.303%
KPIT	0.500052795	3.671532734	1.835960205	0.177612529	17.761%
OFSS	0.132622821	20.35647168	2.699732706	0.261174698	26.117%
Wipro	0.078328925	25.98534823	2.035404392	0.196906948	19.691%
		$\sum Z$	10.33688456		

**It can be inferred from the above analysis that an investor should invest 32.127% in MindTree, 4.30% in Infibeam, 17.761% in KPIT, 26.117% in OFSS and 19.691% in Wipro.**

**Conclusion:**

Sharpe Single index model is a very convenient and crucial for construction of optimum portfolio. The advantage is that this method employs comparatively fewer inputs than Model of Markowitz. Also only one index is used for construction of the portfolio.

Ranking the stocks, finding cut off rate and finding the proportion to be invested. In present study, nine stocks of NSE IT INDEX are used to make an optimal portfolio. Out of these stocks, **investors are advised to invest in five stocks namely 32.127% in MindTree, 4.30% in Infibeam, 17.761% in KPIT, 26.117% in OFSS and 19.691% in Wipro.**

However, the investors should incessantly monitor and track their portfolio due to dynamic nature of the market. Hence it is imperative that investors continuously update their portfolio in consonance with changing market conditions to optimize their returns.

**References: -**

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